



## Evaluating the use of ECG signal in low frequencies as a biometry



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### ARTICLE INFO

**Keywords:**  
Biometrics  
ECG  
Frequency sampling  
Majority voting scheme

### ABSTRACT

Traditional strategies, such as fingerprinting and face recognition, are becoming more and more fraud susceptible. As a consequence, new and more fraud proof biometrics modalities have been considered, one of them being the heartbeat pattern acquired by an electrocardiogram (ECG). While methods for subject identification based on ECG signal work with signals sampled in high frequencies (>100 Hz), the main goal of this work is to evaluate the use of ECG signal in low frequencies for such aim. In this work, the ECG signal is sampled in low frequencies (30 Hz and 60 Hz) and represented by four feature extraction methods available in the literature, which are then feed to a Support Vector Machines (SVM) classifier to perform the identification. In addition, a classification approach based on majority voting using multiple samples per subject is employed and compared to the traditional classification based on the presentation of single samples per subject each time. Considering a database composed of 193 subjects, results show identification accuracies higher than 95% and near to optimality (*i.e.*, 100%) when the ECG signal is sampled in 30 Hz and 60 Hz, respectively, being the last one very close to the ones obtained when the signal is sampled in 360 Hz (the maximum frequency existing in our database). We also evaluate the impact of: (1) the number of training and testing samples for learning and identification, respectively; (2) the scalability of the biometry (*i.e.*, increment on the number of subjects); and (3) the use of multiple samples for person identification.

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### 1. Introduction

The identification of a subject using a unique biological feature, *i.e.*, biometric feature, is very important in the society nowadays. Therefore, the study and development of automatic and accurate systems for such aim are a subject of high interest in the research community. Traditional strategies, such as fingerprinting and face recognition, are becoming more and more susceptible to frauds (Singha, Singhb, & Gupta, 2012). As a consequence, novel fraud proof biometrics modalities have been studied, such as the heartbeat pattern acquired by an electrocardiogram (ECG) (Odinaka et al., 2012). The ECG describes the variation of the electric activity produced by the heart as a function of time, as illustrated in the top row of Fig. 1. Its acquisition is extremely simple and non-invasive, which makes it easy to be employed as a biometry. According to Odinaka et al. (2012), the ECG signal has been studied as a biometry for more than one decade and has shown promising results.

Features extracted from the ECG signal can be categorized into three classes: fiducial, non-fiducial and hybrids of them. The first class considers the fiducial points extracted from the ECG signal,

as in Chazal, O'Dwyer, and Reilly (2004) and Song, Lee, Cho, Lee, and Yoo (2005), which are more affected by the sub-sampling as illustrated in Fig. 1. One can see the lost of information in lower frequencies (*e.g.*, the R peak – the impulse locus). Methods based on non-fiducial features do not use fiducial points directly as features. For example, one can use the fiducial points Q, R and S to create a segment of the heartbeat. The length of the segment is considered a fiducial feature but if the area under the segment is used as a feature, it is considered a non-fiducial feature. Some authors do not use fiducial points to build the non-fiducial features, but segment the ECG signal into several parts that may (Li & Narayanan, 2010) or not (Yu & Chou, 2008) present overlapping. In addition, there are several authors (Güler & Übeyli, 2005; Yu & Chen, 2007) that use a mix of fiducial and non-fiducial features to create the feature vector. Such mix of classes of feature are called hybrids.

The first work using the ECG as a biometry was proposed by Biel, Pettersson, Philipson, and Wide (2001), in which the authors reported an accuracy of 100% to identify 22 subjects using 12 fiducial points in the ECG curve, principal component analysis (PCA) to reduce the dimensionality and a generative model classifier (GMC) to identify the samples. After that seminal work, other methods have been proposed. Irvine, Wiederhold, and Gavshon (2001) reported accuracy of 91% to identify 104 subjects using 15 fiducial

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points chosen by Wilks Lambda Feature Selection and the Linear Discriminant Analysis classifier. Employing PCA and GMC, Zhang and Wei (2006) employed 14 features extracted from the fiducial points, which was able to identify 520 subjects with accuracy of 97.4%. Using an approach based on the wavelet coefficients extracted from ECG, Chiu, Chuang, and Hsu (2008) achieved an accuracy of 95.71% considering 45 subjects. Recently, in Fanga and Chanb (2013), a QRS detection-free ECG biometric based on the phase space trajectory of the ECG signal using a coarse grained-structure was proposed. They performed tests using 100 subjects and the achieved accuracy was 99% when using three-lead ECG. The high accuracies achieved by these works indicate the viability of using ECG as a biometry.

The ECG signal is usually sampled in high frequency (higher than 100 Hz) to capture features associated with cardiac diseases (Luz, Nunes, de Albuquerque, Papa, & Menotti, 2013). For this reason, the equipments that acquire the ECG signal (e.g., Holter), are projected to sample the ECG signal in frequencies higher than 100 Hz. Sidek and Khalil (2013) investigated the impact of the sampling frequency of the ECG signal for the subject identification. In that work, the results showed that the increase in the sampling frequency provides a higher accuracy. However, the authors considered samples with at least 128 Hz and not lower frequencies. To the best of our knowledge, there are no works in the literature that investigate the impact of the sampling in lower frequencies (<100 Hz) to perform subject identification, which will be one of the focus of this work.

This work investigates the viability and reliability of performing identification based on ECG sampled in low frequencies. From the ECG signals sampled in low frequency, four ECG feature extractors are employed to extract representations aiming at identifying subjects using a *Support Vector Machines* (SVM) classifier. Since in identification based on the ECG signal, each sample is a heartbeat, multiple samples of a subject can be acquired in a few seconds. Therefore, this work also evaluates the impact caused by changing the number of samples per subject used during training and testing. In addition, we employ a majority voting scheme since for each subject we can decide his/her identity using several heartbeats instead of a single one because we know that those samples belong to a single, but still unknown, subject. Hence, the evaluation of each sample does not need to be independent, one by one, such as in other biometrics such as picture-based face identification. According to the experimental results, the classification based on multiple samples using a majority voting scheme, referred to as *dependent classification* is more stable and accurate than the traditional classification approach, referred to as *independent classification*. Moreover, the biometry scalability (i.e., increment on the number of subjects) is also evaluated.



**Fig. 1.** ECG signal sampled in low frequencies. In the first row, it is shown the original ECG signal, while in the last two ones the corresponding signal sampled in 60 Hz and 30 Hz, respectively.

The experimental results, presented in Section 3, show the viability of performing subject identification in low sampling frequencies (30 Hz and 60 Hz), which might guide new researches on heart-signal based biometry applications such as the usage of Eulerian Video Magnification (Wu et al., 2012) (at 30 Hz from a video), smart mobile phone and video game control accelerometers (at 60 Hz or higher in practice for iPhone and Wii control) (Kwon, Lee, Chung, & Park, 2011).

The remainder of this work is organized as follows. The evaluation methodology considered in this work is presented in Section 2. In Section 3, the experiments performing the proposed evaluations are described and also a discussion regarding the results is presented. Finally, in Section 4, conclusions are pointed out.

## 2. Evaluation methodology

This section describes the methodology employed for performing the proposed evaluations. First, the ECG signal is sampled in a specific frequency and then it is preprocessed. Then, ECG fiducial points are detected aiming at segmenting each heartbeat so that feature extraction might be executed. Once the features have been extracted, samples are randomly selected and this new set is then split into training and testing sets. The training samples are used to build subject's models with a standard classifier (e.g., SVM), which are employed then to classify the testing samples. The flowchart in Fig. 2 illustrates the methodology and each step of the process is described in details in the following sections. Note that the ECG signal sampling step is omitted here because it is data dependent. It will be discussed in more details when the datasets are described in Section 3.

### 2.1. ECG preprocessing

In the first step, the ECG signal obtained from different databases publicly available are frequency normalized using simple linear interpolation. The preprocessing step aims at reducing the noise from the ECG signal, derived from muscular interference or more commonly from the power grid (50 Hz or 60 Hz). Finite impulse response (FIR) recursive digital filters are the mostly used for attenuation of these noises. In addition, signal amplitude normalization is also performed in the preprocessing step.

### 2.2. Heartbeat segmentation

The ECG segmentation consists of delimiting the heartbeat most interesting part, the QRS complex, its points (Sayadi & Shamsollahi, 2009), and other interesting fiducial points such as P and T points and the segments related to them. Such information is used by feature extraction techniques. Once the QRS complex and fiducial points are segmented, one can obtain several physiological information such as the heart rate, length and amplitude of pulse. For performing the heartbeat segmentation task, there are in the literature algorithms with accuracy near to the optimality (i.e., almost 100%) (Afonso, Tompkins, Nguyen, & Luo, 1999; Hu, Tompkins, Urrusti, & Afonso, 1990; Pan & Tompkins, 1985; Sayadi & Shamsollahi, 2009). However, in this work, we use databases in which this information was previously annotated.

### 2.3. Feature extraction

To evaluate different representations, four distinct set of features are extracted from the ECG signal. These sets were selected from works that use techniques largely disseminated in the literature for representing a heartbeat to classify arrhythmia, in which the goal is to discriminate/classify a single heartbeat of a subject,

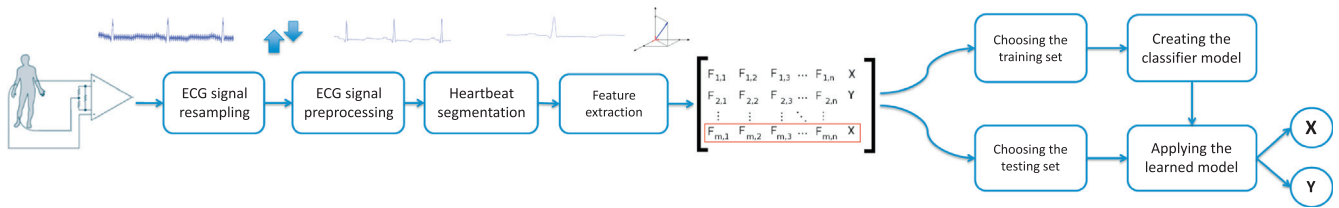


Fig. 2. Flowchart of the subject identification system from ECG signals used in this work.

i.e., a single sample (Güler & Übeyli, 2005; Song et al., 2005; Yu & Chen, 2007; Yu & Chou, 2008). The feature extraction methods considered in this work are detailed in the next paragraphs.

Song et al. (2005). The authors used the wavelet transform to extract 15 features of each heartbeat. The wavelet transform allows the analysis of the signal in both time and frequency domain (Mallat, 1999). The heartbeat is represented by a 400 ms window of sampling points from ECG signal around the R peak. This discrete curve composed by these points is decomposed in seven levels of wavelet transform, in which only the detail subbands are used. Along with these wavelet features, other two features from the RR interval (temporal distance between the peak (R point) of two consecutive heartbeats/points): the RR interval between the current beat and its predecessor (RR-predecessor), the RR interval between the current beat and its successor (RR-posterior); were included to the feature vector, resulting in 37 features.

Güler and Übeyli (2005). The authors also used the wavelet transform to decompose a ECG signal of 700 ms approximately surrounding the R peak in four detail and one approximation subbands. In order to reduce the dimensionality to 19 features, the authors have proposed the use of statistical techniques: absolute mean, standard deviation and power of the coefficients in each wavelet subband, besides the ratio of the absolute mean of the underlying subbands. The researchers highlighted that the choice of the mother Wavelet function used for feature extraction is crucial for the final effectiveness of the classification model. Thus, all methods re-implemented in this work that use the wavelet transform were carefully reproduced taking into account the same wavelet transform and mother function originally proposed by the authors of those works.

Yu and Chen (2007). In the work proposed in Yu and Chen (2007), the authors used statistical techniques directly on heartbeat samples and, also, in three wavelet sub-bands: details of the first level of wavelet transform decomposition and approximation and details of the second level one. It is also used the AC power of the original signal, the AC power of each wavelet sub-band, the AC power of the autocorrelation function of the coefficients of each sub-band, and the ratio between the maximum and minimum values in each sub-band, adding up to 12 features. Besides these 12 statistical features, the authors also used the RR interval (RR-predecessor).

Yu and Chou (2008). The authors used *Independent Component Analysis* (ICA) for extracting 100 coefficients of a heartbeat composed of 200 sampling points centered at the R peak. The ICA coefficients are computed using the linear *Fast-ICA* algorithm proposed in Hyvärinen (1999) and only the 33 first coefficients are used. According to these researchers, the ICA is used to decompose the original ECG in a weighted sum of the components that are statistically and mutually independents. Besides these coefficients, it is included the RR interval (RR-predecessor), adding up to 34 features.

#### 2.4. Sample classification

Usually, the effectiveness of subject identification methods is measured using the accuracy of heartbeat classification. In this

work, we propose to evaluate the effectiveness of this system using a majority voting scheme since for each subject we can decide his/her identity using several heartbeats instead of a single one. Thus, in this work, we use two measures of accuracy in order to determine the subject identification effectiveness. The first, referred to as *independent classification*, is based on the traditional and independent approach in which the accuracy is calculated as the number of correctly classified heartbeat over the total number of heartbeats. The second, referred to as *dependent classification*, is based on a majority voting scheme considering the classification of a sequence of consecutive samples (heartbeats) obtained from a subject. A subject being classified for the dependent classification approach has assign the identity that appears the maximum number of times, considering all his/her samples collected during one section.

After the feature extraction, a classification model is learned using the SVM algorithm (Cortes & Vapnik, 1995; Schölkopf & Smola, 2002) using a training database. This model is then used to evaluate a testing database. The SVM has been chosen as learning algorithm since it is one of the most popular classifiers found in the literature and it has reported promising results for subject identification using ECG signal (Li & Narayanan, 2010; Ye, Coimbra, & Kumar, 2010).

#### 2.5. Computational complexity

The computational complexity of this methodology is as follows. All processes (ECG signal sampling, ECG signal preprocessing, heartbeat segmentation, and feature extraction), developed for predicting/identifying a sample/subject, have linear time complexity with respect to the number of sampled points in the ECG signal, except the classification phase, which is bounded by the type of the kernel used in the SVM and the support vectors learned on the training phase.

The learning phase, which involves the same steps of the prediction phase except the training phase, depends on the SVM algorithm, which is cubic in the worst case with respect to the training set and feature vector sizes. The implementation of the majority voting scheme using buckets for subject votes has also linear time complexity regarding the number of possible subjects to be classified. Although the methodology described does not present a final linear time complexity, its runtime for evaluating heartbeats is suitable for real-time applications.

### 3. Experimental evaluation

In this section, we evaluate different sampling frequencies described by different feature extraction methods to assess the feasibility of ECG-based recognition in low sampling frequencies, such as 30 and 60 Hz. In addition, we evaluate the employment of the majority voting scheme (*dependent classification*) to subject identification, the scalability of ECG signals by varying the number of subjects and the impact in the accuracies when changing the number of training and testing samples for learning and identification, respectively.

### 3.1. The databases and experimental setup

There are several publicly available databases for evaluating systems aiming at the identification of patterns in ECG signals. Nonetheless, other non public databases have been also used in several studies. The popular databases are available in Physionet's web (Moody & Mark, 2001) and in this work we chose four databases from there: MIT-BIH Arrhythmia (MITDB), MIT-BIH Supraventricular Arrhythmia Database (MITSUP), MIT-BIH Normal Sinus Rhythm (NSRDB), and European ST-T (EDB).

The MITDB database contains 48 records of heartbeats, each one of approximately 30 min, sampled in 360 Hz, belonging to 47 different patients/subjects (there are two records for a same patient). These records were chosen from a set of more than 4000 patient's records using *holters* of the Beth Israel Hospital Arrhythmia Laboratory (today Beth Israel Deaconess Medical Center) from 1975s until 1979s. 23 out of 48 were randomly chosen from this large set. To obtain a balanced sampling of patients with varied heart diseases (*i.e.*, arrhythmia), the remaining 25 records (to accomplish 48) were carefully selected. Among these 25, rare and hard to classify disease type situations were chosen in order to create a database with very different conditions. The ECG signals were acquired from 25 men varying between 32 and 89 years old and 22 women from 23 to 89 years old. Note that this database is the most researched one for arrhythmic studies.

The MITSUP database comprises 78 records of patients, with 30 min of duration each, sampled in 128 Hz, and has been proposed to be a complement of the MITDB. Its records also were obtained using *holters* of the Beth Israel Hospital Arrhythmia Laboratory in the same epoch.

The NSRDB database includes records of 18 subjects acquired in the Arrhythmic Laboratory of the Beth Israel Hospital. These subjects were chosen to compose this database because they had no "visible" heart disease, that is, they had a healthy heart. This database is composed of records from 5 men (from 26 to 45 years old) and 13 women (from 20 to 50 years old). All these records were sampled in 128 Hz.

The EDB database is a collection of 90 records acquired from 79 subjects, sampled in 250 Hz. These records were extracted from 70 men (from 30 until 84 years old) and 8 women (from 55 until 71 years old). As all of these subjects were suffering from a specific cardiac disease (*i.e.*, myocardial ischemia), the database was originally built to allow ST-segment and T-wave analysis.

Table 1 summarizes these figures with respect to the databases. It is important to note that: (1) Subjects with duplicated records are present in the MITDB and EDB databases and one of each duplicated record was discarded; (2) Records of subjects/patients using pacemakers were not selected; (3) Records of subjects/patients containing in majority arrhythmic heartbeats were not selected as well. Thus, those records of such subjects were not used, resulting then on 193 subjects/records for our experiments.

The aforementioned databases were chosen mainly because they were made using the same type of *holter* for acquiring the ECG signal of all subjects. In contrast, as the frequency sampling of these databases are different (see Table 1, in Freq. column), it was required a frequency normalization process as stated in

previous sections. Indeed, all records were re-sampled using the maximum frequency among the database (360 Hz) by employing a simple linear interpolation process before the preprocessing phase of our methodology.

All experiments performed in this work were executed 30 times. Each time, an experimental set was created by choosing samples randomly from  $n$  initially specified subjects to generate the training and testing sets. That is, for each run of an experiment set, the subjects used were randomly chosen from the database composed of 193 records. For each subject, a sequence of consecutive samples (heartbeats) are randomly chosen as well. The average ( $\mu$ ) and standard deviation ( $\sigma$ ) of the effectiveness (*i.e.*, accuracies) were computed. In Figs. 3 and 4, confidence intervals using 5% significance level are indicated as vertical bars in the plots and are built based on  $\mu \pm \sigma$ . For the SVM, the regularization and the hyper-parameter for the RBF kernel were always set to  $C = 10$  and  $\gamma = 1/(8f)$ , in which  $f$  is the dimension of the feature vector used. It is important to note that all implementation codes in Matlab and datasets used in this work are publicly available.<sup>1</sup>

### 3.2. Experimental results

To evaluate the application of ECG as a biometry to more realistic scenarios, we performed five types of experiments assessing different aspects of the identification: (1) feature extraction and the sampling frequency; (2) the number of samples used for training and testing; (3) the majority voting scheme (*dependent classification*) compared to the independent classification; (4) the scalability of such biometric as a function of the number of subjects considered; and (5) sampling in lower frequencies.

It is important to remember that we used the overall accuracy as the evaluation metric computed in two ways: (1) traditional one (*independent classification*): the number of correctly classified samples divided by the number of samples presented to the system; (2) employing a majority voting scheme among multiple samples of a same subject classified by the system (*dependent classification*).

**Feature extraction and sampling frequency.** In this experiment, we evaluate four feature extraction sets and different sampling frequencies (20 Hz, 30 Hz, 60 Hz, 120 Hz, 200 Hz, and 360 Hz), aiming at verifying their influence in the overall accuracy using 180 subjects/records (randomly chosen from the entire database composed of 193 records), 128 heartbeats (samples) from each subject for both training and testing. We have chosen 128 samples for testing/training as the maximum expected time (2 min or 120 s) that a person should be exposed for the subject identification process. The results are shown in Table 2 and indicate that higher sampling frequencies result in higher accuracy to identify a subject, as expected. Note that, in this experiment, we employed the independent/traditional classification approach for computing the overall accuracy.

According to Table 2, experiments performed with the feature extraction method proposed by Song et al. (2005) show that the accuracy becomes stable when the sampling frequency reaches 60 Hz. The results obtained by the feature extraction proposed by Güler and Übeyli (2005) drops under 360 Hz and dramatically drops under 60 Hz. Finally, the results obtained by the feature extractions proposed by Yu and Chen (2007) and Yu and Chou (2008) are not promised. Moreover it was not possible to extract features for these two feature extraction methods in low frequencies (60, 30, and 20 Hz) since more points than available are required. Due to that, the accuracies for such configurations are indicated as "–".

**Table 1**  
Statistics summary of the databases used.

Database	Records/subjects	Chosen records	Duration	Freq. (Hz)
MITDB	48/47	43	30 min	360
MITSUP	78/78	64	30 min	128
NSRDB	18/18	18	24 h	128
EDB	90/79	68	02 h	250

<sup>1</sup> <https://code.google.com/p/ecg-biometric/>.



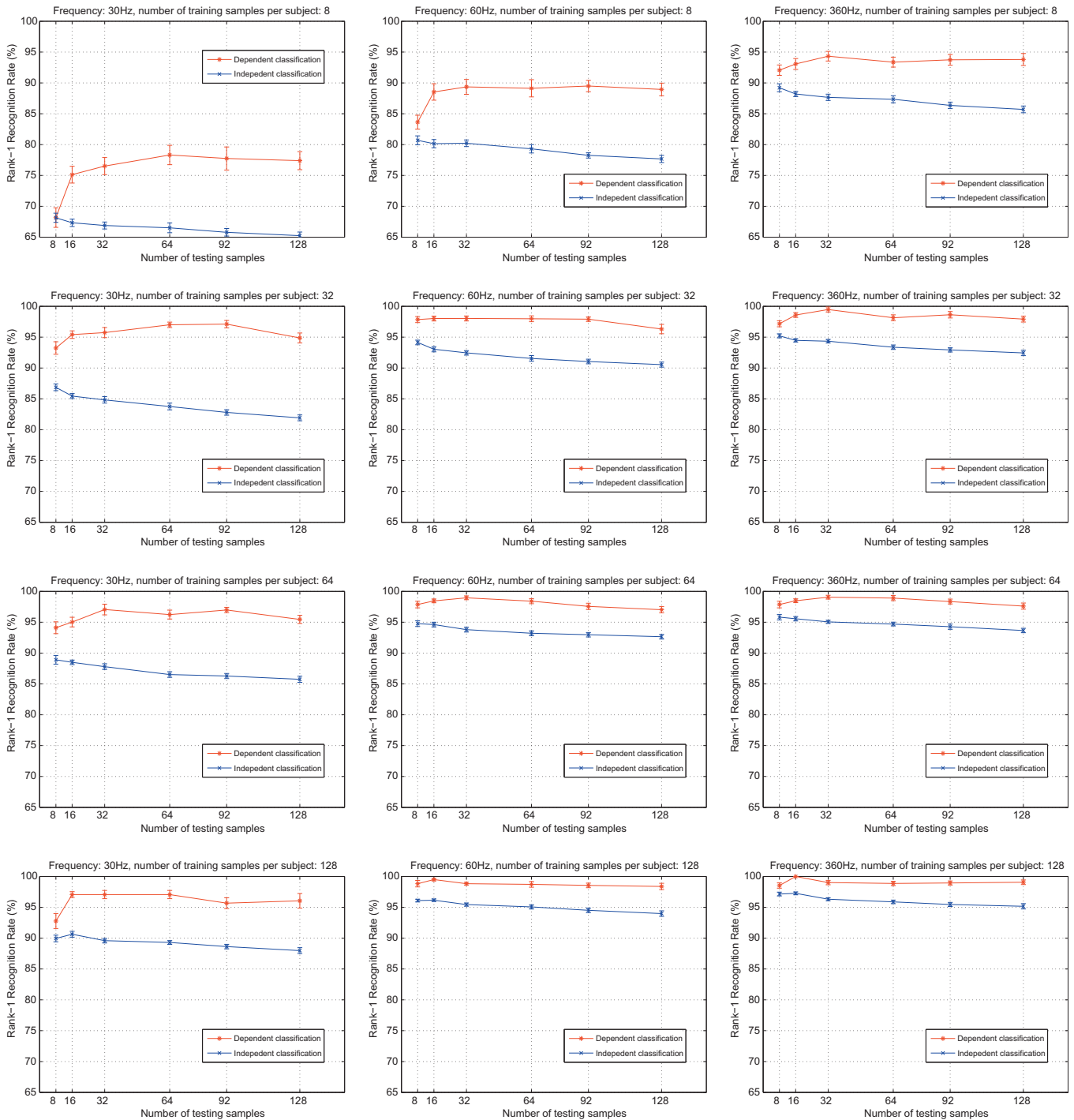


Fig. 3. ECG-based identification evaluation. Number of training and testing samples, majority voting, and frequency sampling.

From the figures in Table 2, we can observe that the accuracies obtained in low frequencies (20 Hz, 30 Hz, and 60 Hz) using the feature sets proposed in Song et al. (2005) and Güler and Übeyli (2005) for subject identification indicate promising results for discriminating subjects using the ECG signal. As the focus of this work is on low frequencies and high values of accuracy (>85%) the remaining experiments and evaluations consider only frequency sampling in 30 Hz or higher and only the feature extraction method proposed in Song et al. (2005).

**Number of samples for training and testing.** This experiment aims at evaluating the influence of the number of samples used for learning and for identification. Fig. 3 shows the results achieved

with different number of training (each row) and testing samples (x-axis of the plots). As a result, for a fixed sampling frequency (columns of the Fig. 3), we can see that the more training samples are used, the more accurate the results are (for both types of accuracy measures), which is an intuitive result since more information is being used. On the other hand, when a large number of testing samples are considered, the accuracy tends to reduce slightly. It is important to observe that, in general, the independent classification approach (accuracy measured in traditional way) decreases slightly with the increase of testing samples. Nonetheless, the dependent classification approach implemented using the majority voting scheme achieves, in general, its highest scores using 16 or

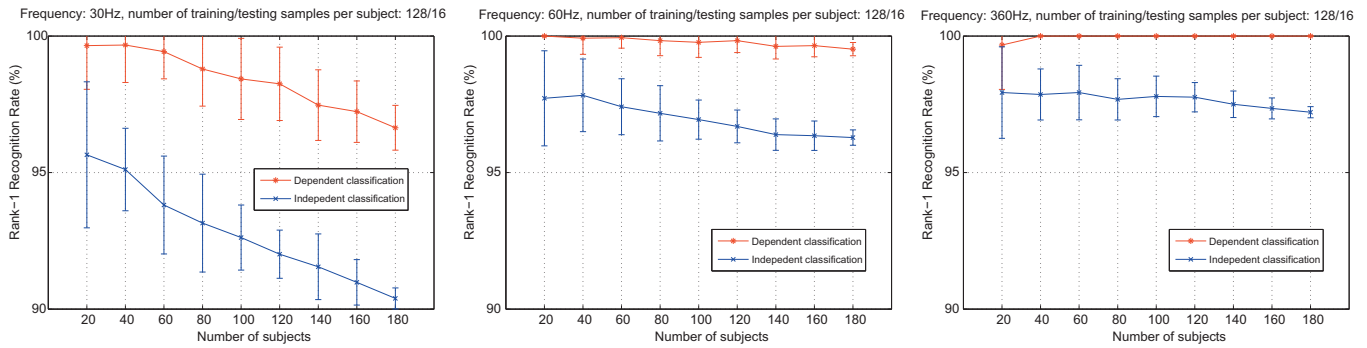


Fig. 4. Scalability evaluation. The recognition rate as a function of the number of subjects, varying from 20 to 180.

Table 2

Evaluation of the four feature extraction methods using 180 subject (randomly chosen from 193) and 128 samples for both training and testing. Each experiment was performed 30 times reporting its mean and standard deviation accuracy ( $\mu \pm \sigma$ ). 1 – Song et al. (2005), 2 – Güler and Übeyli (2005), 3 – Yu and Chen (2007), 4 – Yu and Chou (2008).

Freq. (Hz)	Methods (accuracy in %)			
	1	2	3	4
20	76.5 $\pm$ 0.1	13.1 $\pm$ 4.9	–	–
30	87.5 $\pm$ 0.1	12.4 $\pm$ 7.9	–	–
60	93.6 $\pm$ 0.0	70.5 $\pm$ 0.2	–	–
120	94.5 $\pm$ 0.0	76.4 $\pm$ 0.2	17.52 $\pm$ 0.1	30.96 $\pm$ 0.1
200	94.9 $\pm$ 0.1	78.7 $\pm$ 0.2	18.01 $\pm$ 0.1	39.11 $\pm$ 0.1
360	94.7 $\pm$ 0.1	86.4 $\pm$ 0.1	30.12 $\pm$ 0.1	33.19 $\pm$ 0.3

32 testing samples and its decrease rate with the increasing of testing samples is softer than the independent classification one. In some cases, the dependent classification accuracy is kept slightly as the same.

**Majority voting.** The usage of a majority voting scheme for computing the accuracy (here called dependent classification) is possible in identification using ECG signal since several samples (heartbeats) can be collected from a subject in a small period of time and presented at once to the system because it is known that they belong to the same subject. Fig. 3 shows the results achieved when the dependent classification (using majority voting scheme) is employed (red<sup>2</sup> curves) compared to the independent evaluation of each sample (blue curves). The dependent classification approach achieves higher recognition rates in the vast majority of the results (except in the top-left plot when the frequency is 30 Hz with 8 training and testing samples). In addition, the results indicate that after a certain number of testing samples, the accuracy does not improve (32 samples), which means that the subject would need to stay no more than 30 s to be identified with high accuracy.

**Scalability of the biometric system.** The results shown in Fig. 4 evaluate the scalability of the system as a function of the number of subjects, comparing the dependent classification (majority voting scheme) to the independent classification. As intuitively expected, in general, the accuracy reduces when more subjects are considered. However, for 60 Hz, when the dependent classification is considered, the reduction with the addition of new subjects is slower and even with 180 subjects, the accuracy is still promising (>99%). In particular, for 360 Hz both measures of accuracy does not have significant changes when the number of subjects is increased.

**Frequency sampling comparison.** It is also important to evaluate the impact in accuracy when the sampling frequency is reduced. Comparing column-wise the results shown in Fig. 3, we can see that, in general, the accuracy increases with the frequency. However, we can also say that the results obtained for ECG signal when sampled in 60 Hz are very close (or equivalent) to the ones in 360 Hz, when 64 or 128 training samples are used. Moreover, the dependent classification accuracy measure shows values higher than 95% when the frequency is sampled in 30 Hz, trained with 64 or 128 samples, and tested with more than 16 samples. These results, therefore, demonstrate the viability and reliability of performing subject identification using low frequency sampled ECG (30 Hz and 60 Hz).

#### 4. Conclusions

In this work, we investigated several aspects of the subject identification problem based on ECG signal sampled in multiple frequencies. However, promising results were presented when using low frequencies for discriminating the subjects. In our experiments, the identification accuracy obtained for 180 subjects using the ECG signal sampled in 30 Hz and 60 Hz is greater than 95% and near to, respectively. Such results might allow new researches on heart-signal based biometry applications based on techniques such as Eulerian Video Magnification (Wu et al., 2012) using videos captured in 30 Hz. A second important result is the one obtained with the majority voting scheme, referred to as *dependent classification*, providing high accuracy when several samples for a subject are classified at once.

#### Acknowledgments

The authors would like to thank FAPEMIG, FAPESP, CAPES, and CNPq for the financial support.

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<sup>2</sup> For interpretation of color in Figs. 2–4, the reader is referred to the web version of this article.

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